

Chapter 9

Priority Queues

9.1 Priority Queues (`p_queue`)

1. Definition

An instance Q of the parameterized data type $p_queue<P, I>$ is a collection of items (type pq_item). Every item contains a priority from a linearly ordered type P and an information from an arbitrary type I . P is called the priority type of Q and I is called the information type of Q . If P is a user-defined type, you have to define the linear order by providing the compare function (see Section 2.3). The number of items in Q is called the size of Q . If Q has size zero it is called the empty priority queue. We use $\langle p, i \rangle$ to denote a pq_item with priority p and information i .

Remark: Iteration over the elements of Q using iteration macros such as *forall* is not supported.

```
#include < LEDA/core/p_queue.h >
```

2. Types

$p_queue<P, I>::item$ the item type.
 $p_queue<P, I>::prio_type$ the priority type.
 $p_queue<P, I>::inf_type$ the information type.

3. Creation

$p_queue<P, I> Q;$ creates an instance Q of type $p_queue<P, I>$ based on the linear order defined by the global compare function $compare(const P\&, const P\&)$ and initializes it with the empty priority queue.

$p_queue<P, I> Q(int (*cmp))(const P\&, const P\&);$

creates an instance Q of type $p_queue<P, I>$ based on the linear order defined by the compare function cmp and initializes it with the empty priority queue. *Precondition:* cmp must define a linear order on P .

4. Operations

$const P\& Q.prio(pq_item it)$ returns the priority of item it .
Precondition: it is an item in Q .

$const I\& Q.inf(pq_item it)$ returns the information of item it .
Precondition: it is an item in Q .

$I\& Q[pq_item it]$ returns a reference to the information of item it .
Precondition: it is an item in Q .

$pq_item Q.insert(const P\& x, const I\& i)$
 adds a new item $\langle x, i \rangle$ to Q and returns it.

$pq_item Q.find_min()$ returns an item with minimal priority (nil if Q is empty).

$P Q.del_min()$ removes the item $it = Q.find_min()$ from Q and returns the priority of it.
Precondition: Q is not empty.

$void Q.del_item(pq_item it)$ removes the item it from Q .
Precondition: it is an item in Q .

$void Q.change_inf(pq_item it, const I\& i)$
 makes i the new information of item it .
Precondition: it is an item in Q .

$void Q.decrease_p(pq_item it, const P\& x)$
 makes x the new priority of item it .
Precondition: it is an item in Q and x is not larger than $prio(it)$.

$int Q.size()$ returns the size of Q .

$bool Q.empty()$ returns true, if Q is empty, false otherwise.

$void Q.clear()$ makes Q the empty priority queue.

5. Implementation

Priority queues are implemented by binary heaps [91]. Operations `insert`, `del_item`, `del_min` take time $O(\log n)$, `find_min`, `decrease_p`, `prio`, `inf`, `empty` take time $O(1)$ and `clear` takes time $O(n)$, where n is the size of Q . The space requirement is $O(n)$.